



WAKE FOREST  
UNIVERSITY



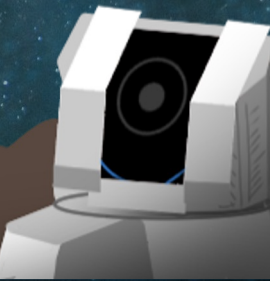
# Multimessenger Astrophysics

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Caitlin A. Witt

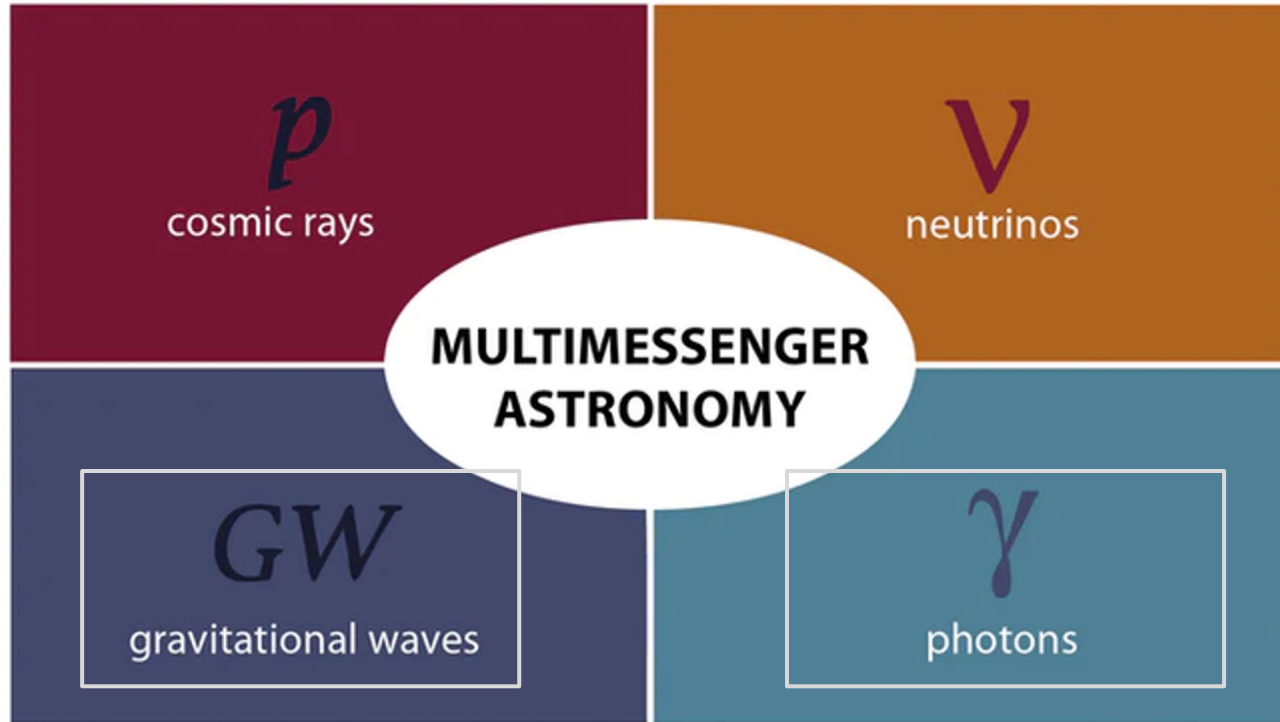
Assistant Professor of Physics  
Wake Forest University

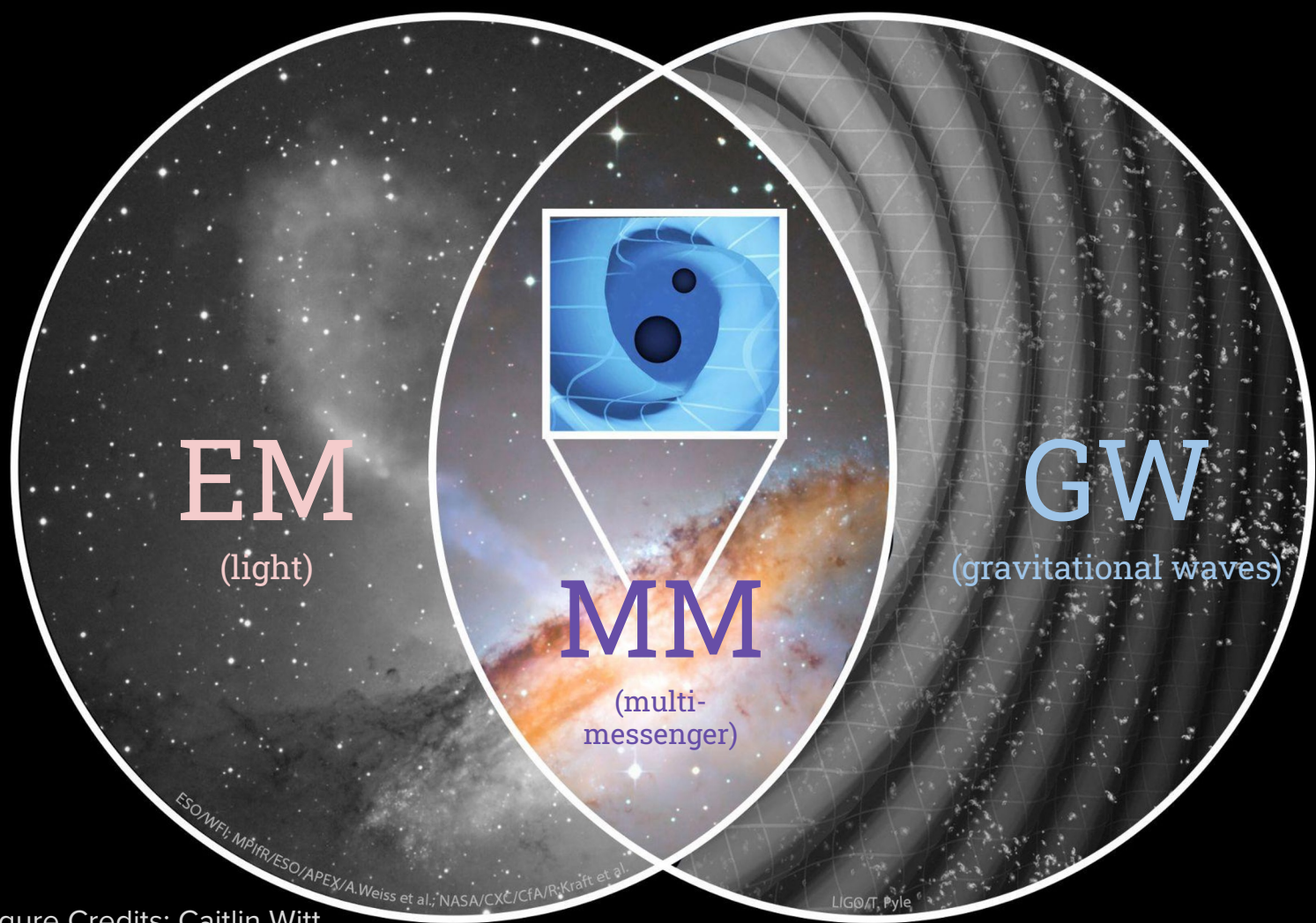
[wittc@wfu.edu](mailto:wittc@wfu.edu)

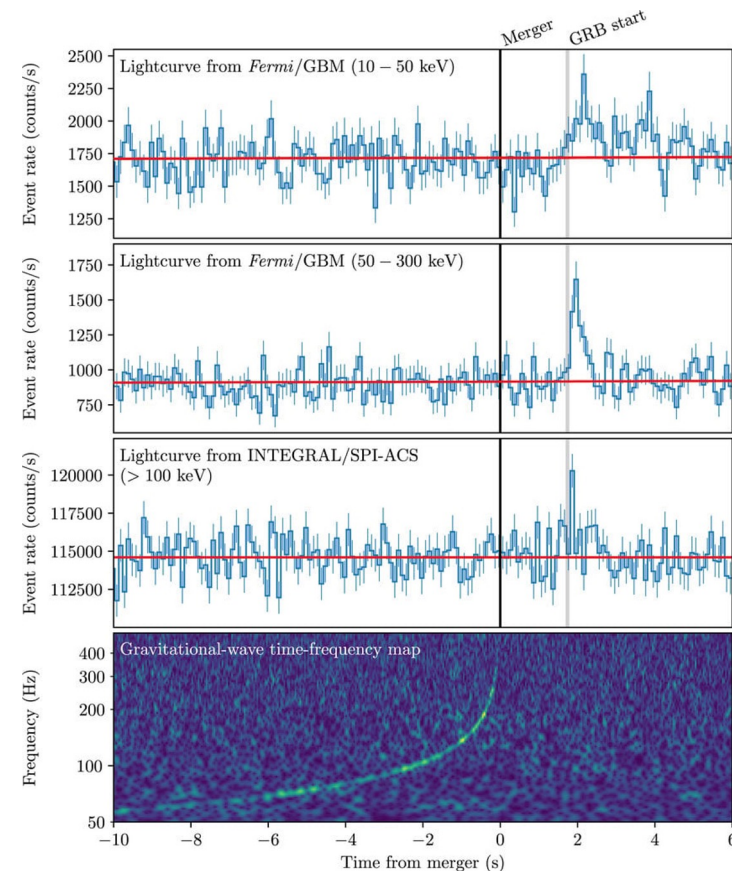
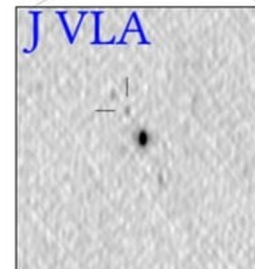
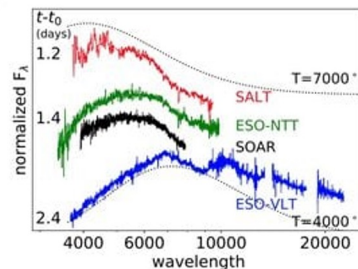
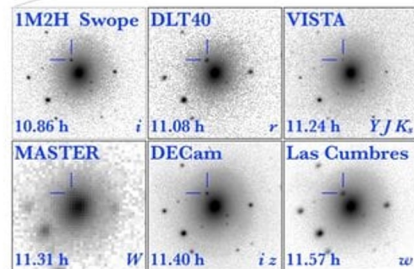
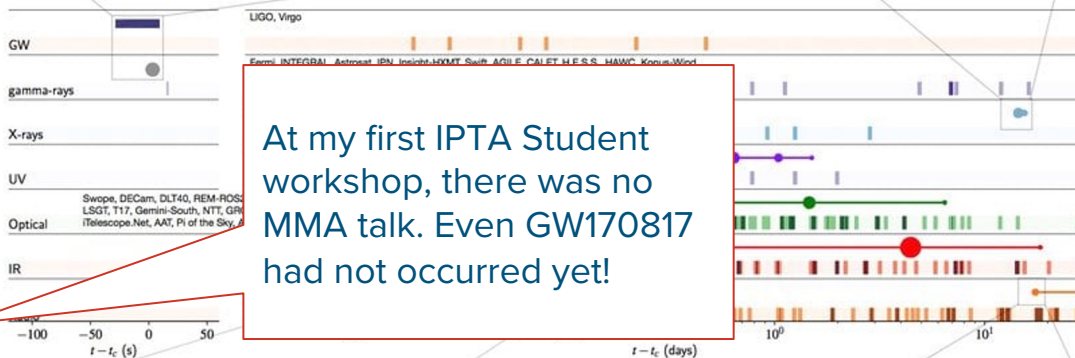
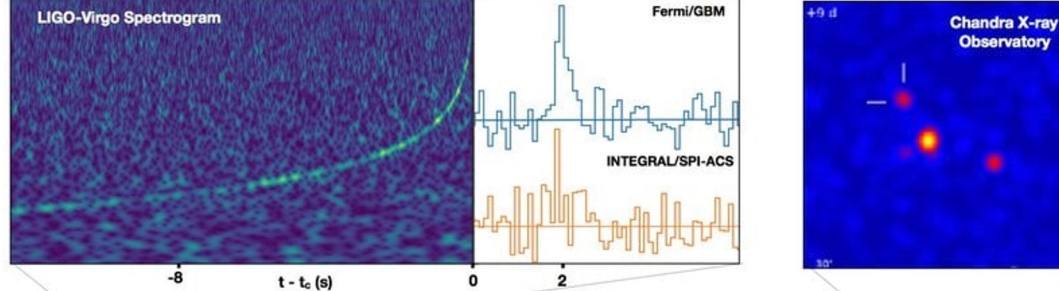


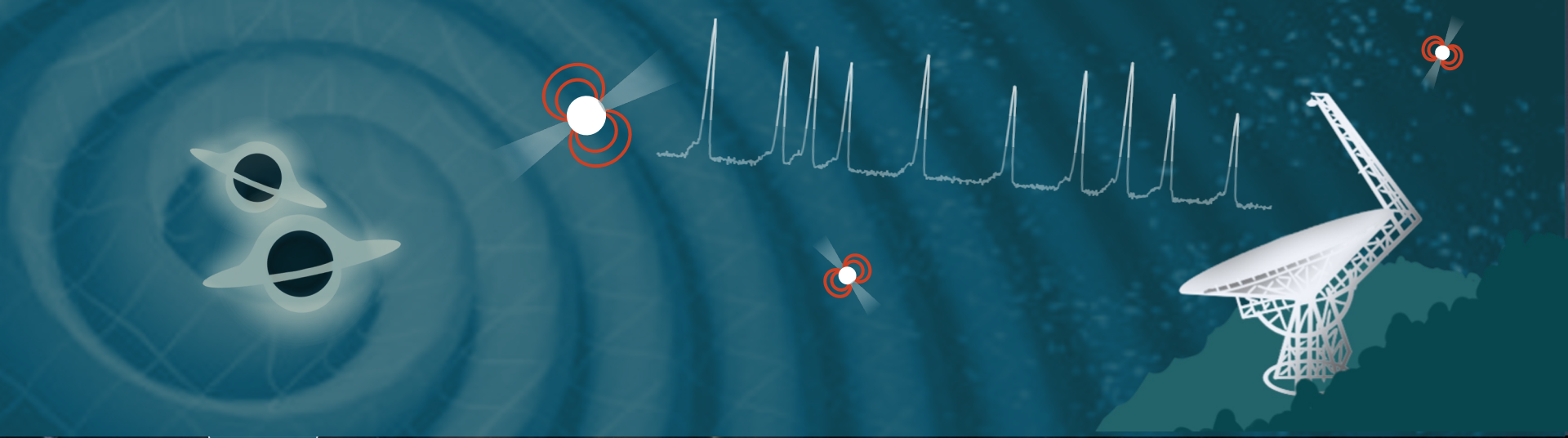
# “Multi-Messenger”?

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PTAs aim to detect GWs  
and study SMBHBs

# If pulsar science is a safari...

SMBHB observations are  
landscape photography

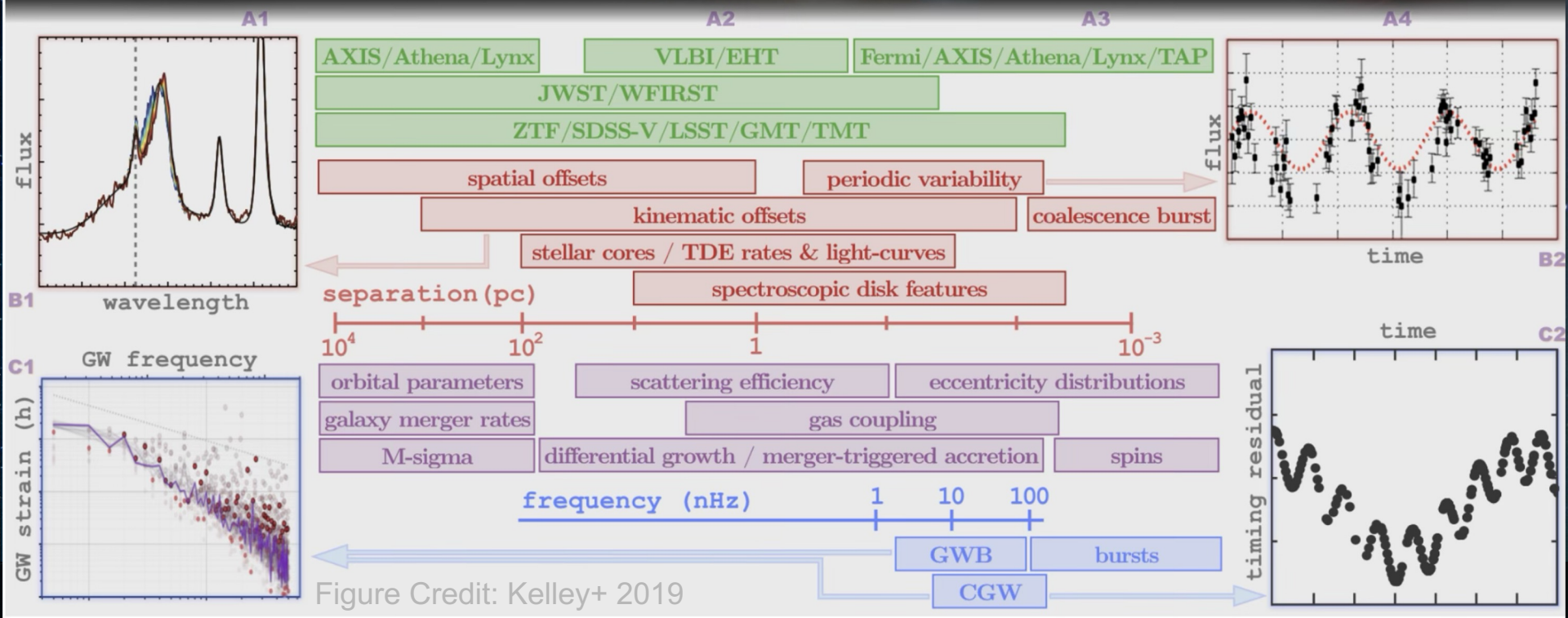
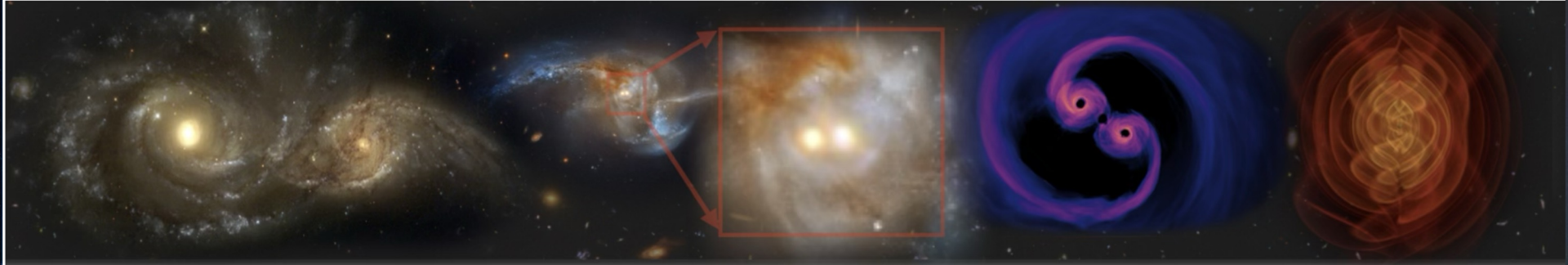


And MMA puts the two  
together to study the whole  
ecosystem

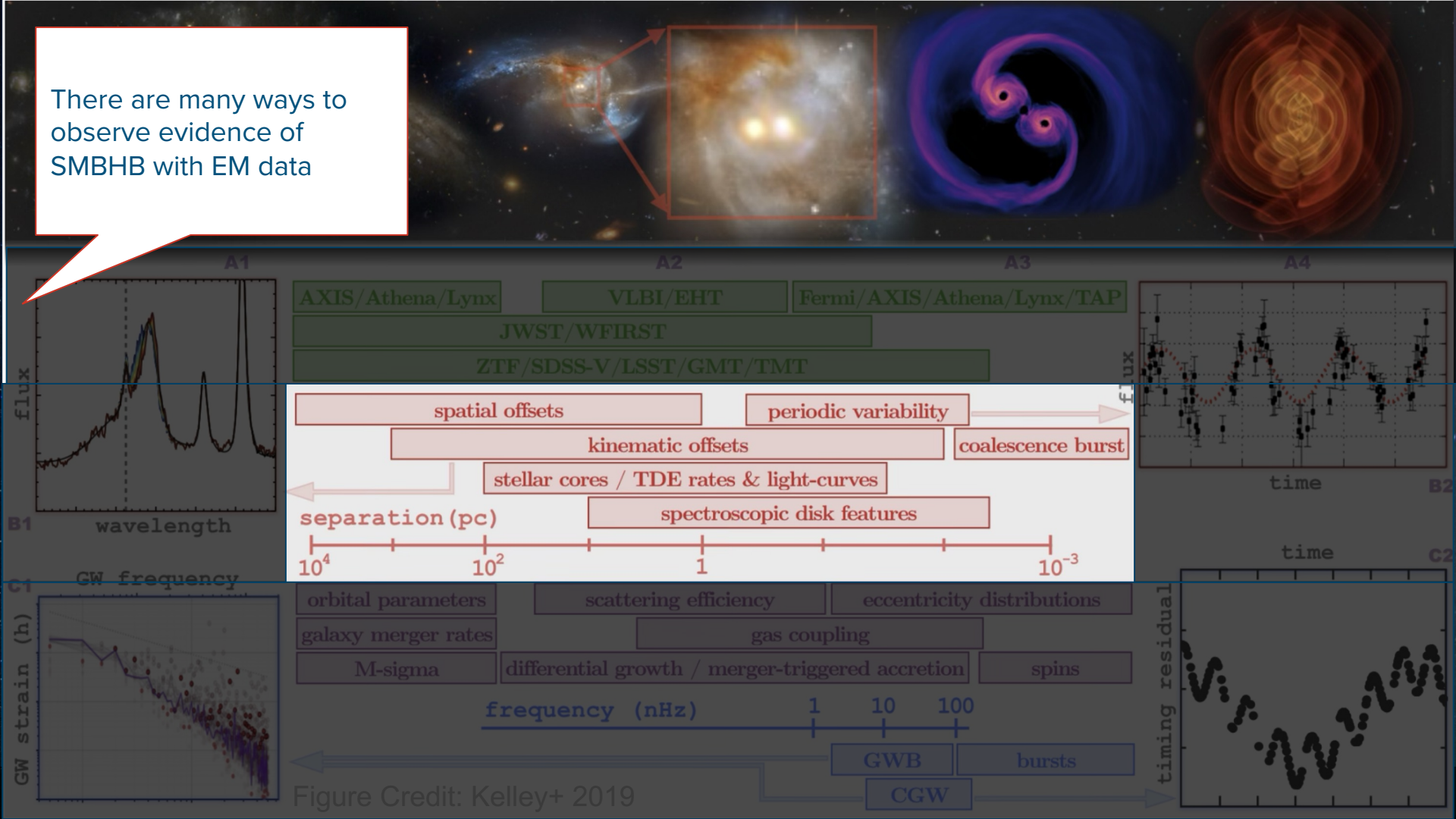




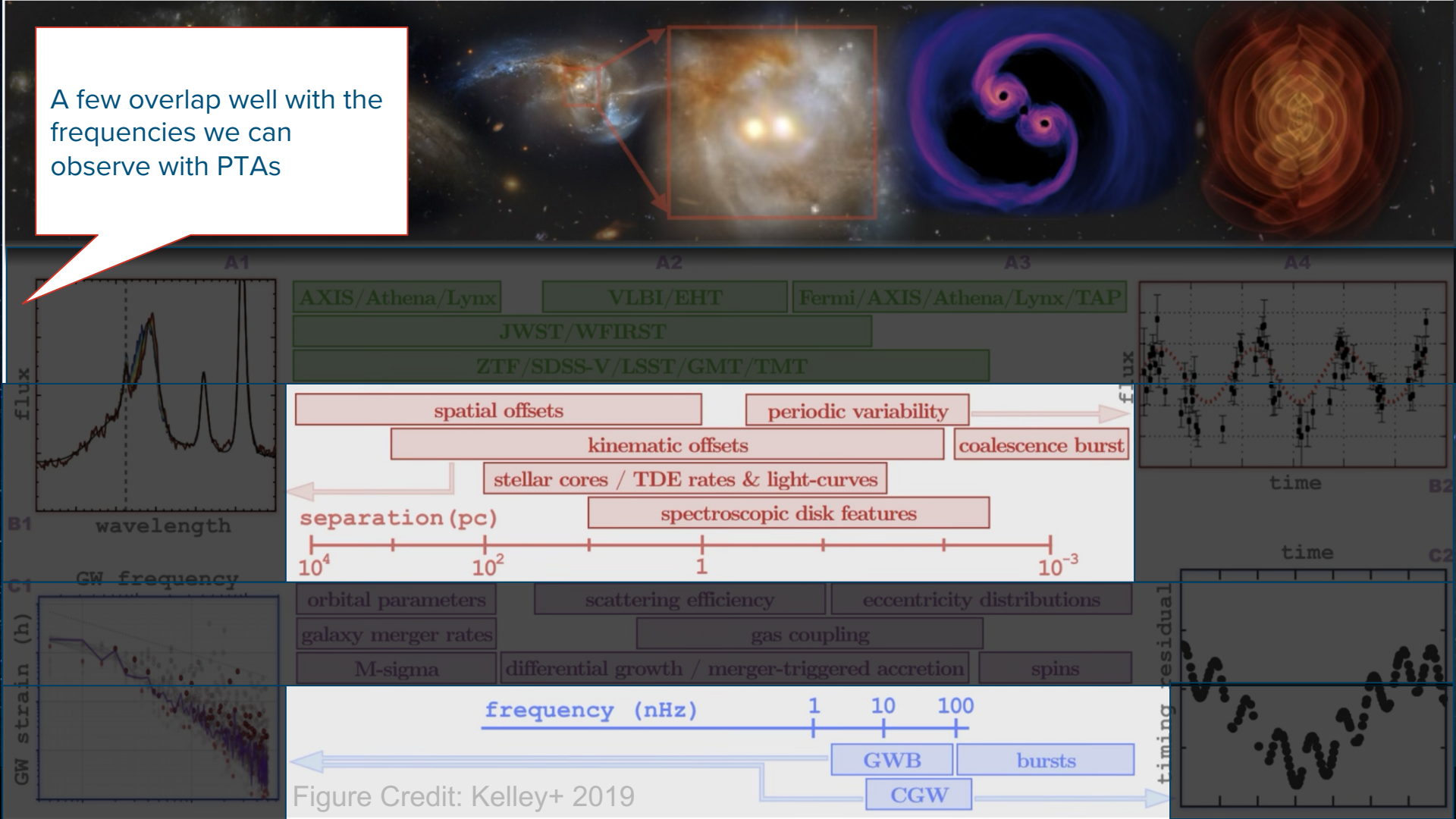
# Multi-Messenger Astrophysics

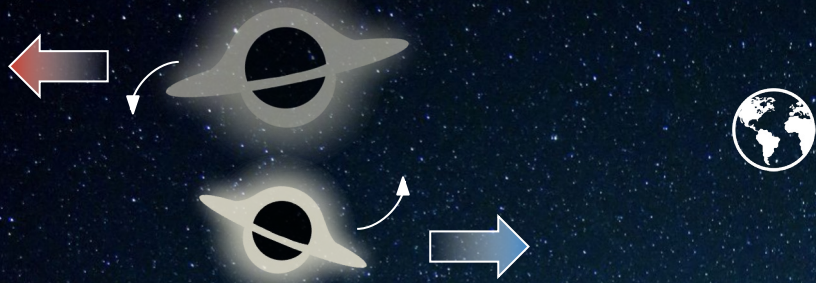


There are many ways to observe evidence of SMBHB with EM data

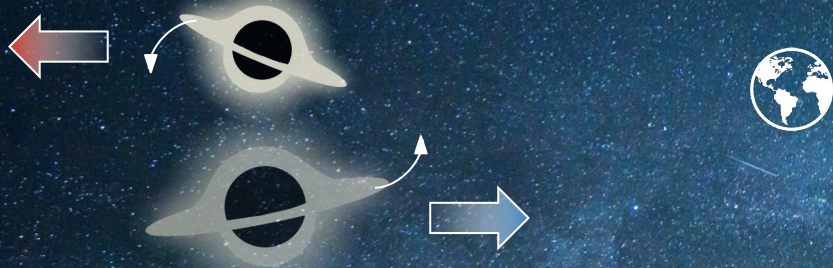


A few overlap well with the frequencies we can observe with PTAs



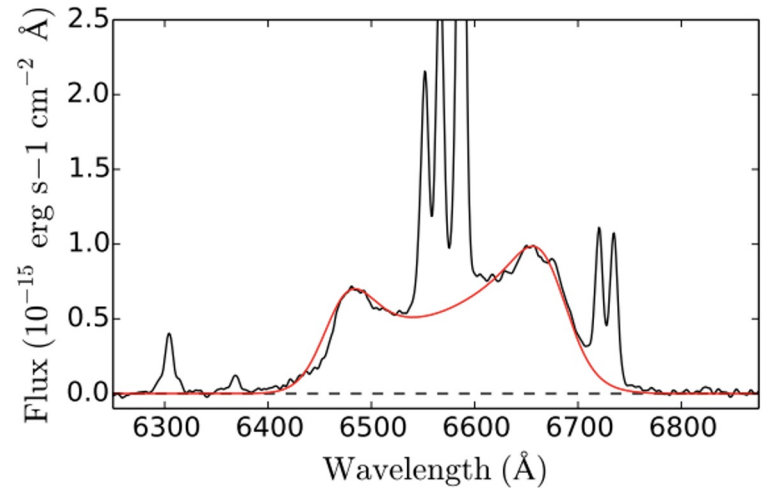


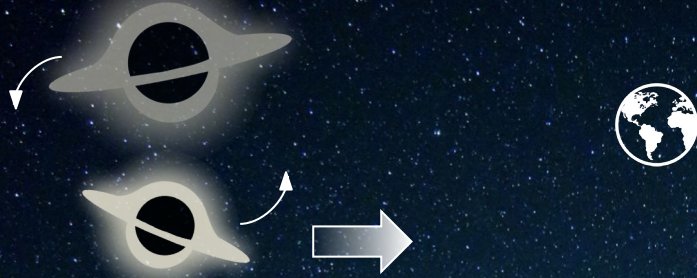
Broad line regions red- and blue-shift periodically



## Double Broad Lines

As SMBHs orbit, spectrum evolves over time



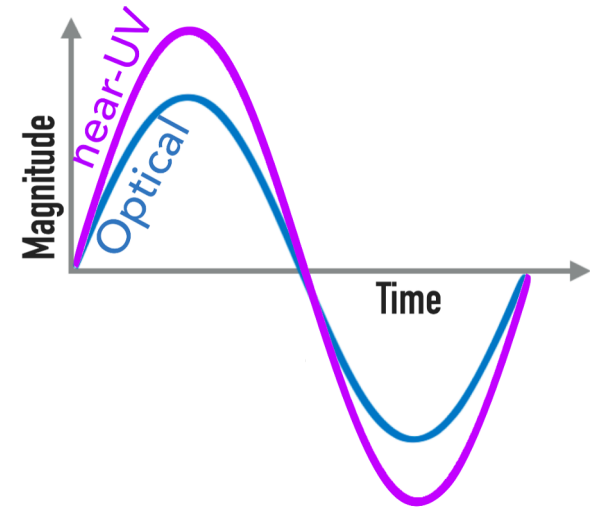


Light gets brighter or dimmer from relativistic orbital motion of SMBHs

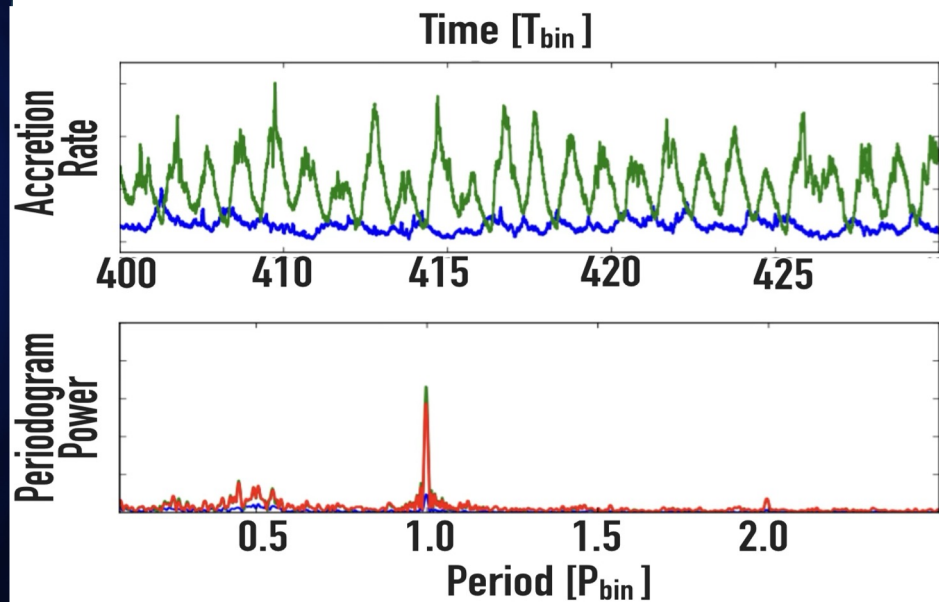
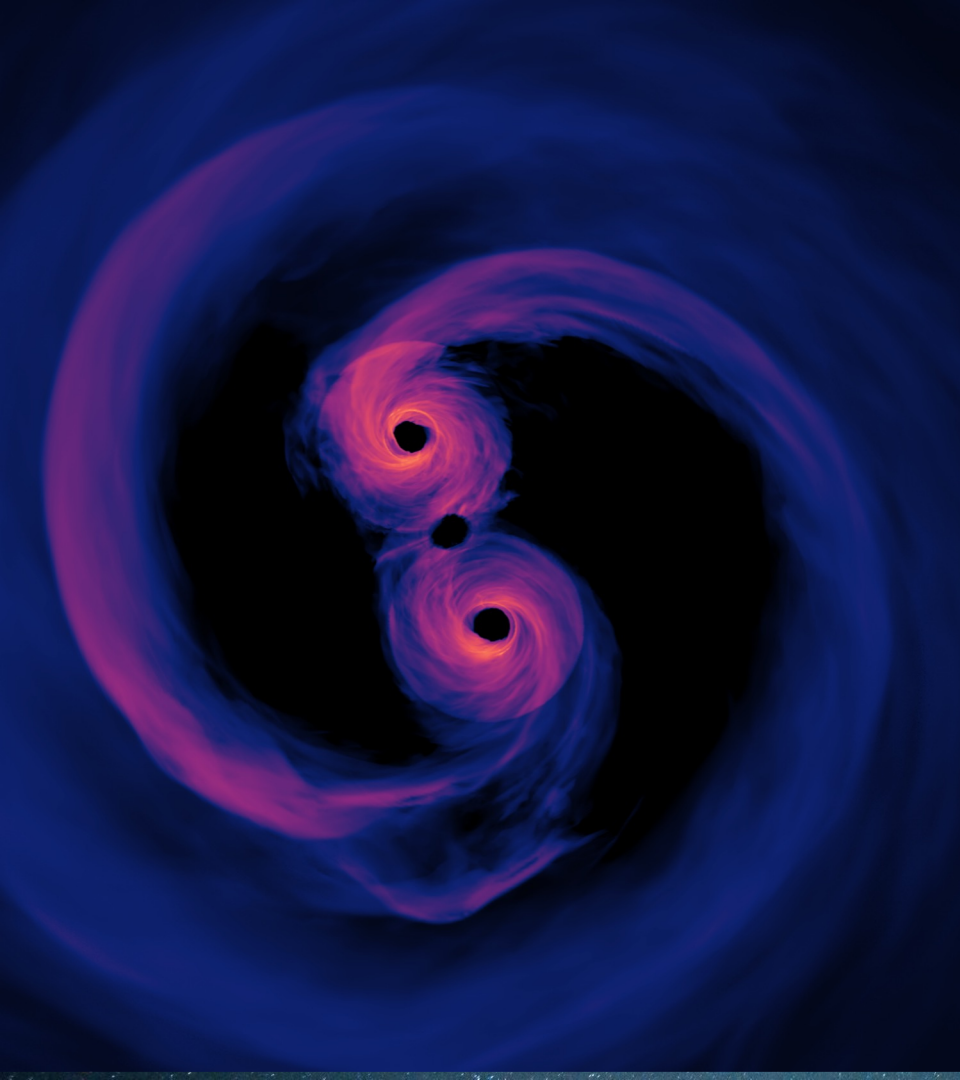


# Periodic Doppler Boost

Over time, this creates a periodic change in the brightness of the quasar

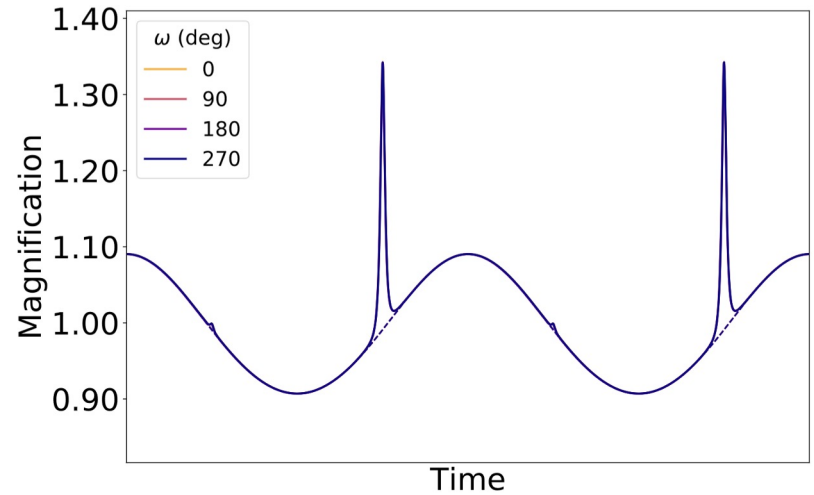


# Periodic Accretion

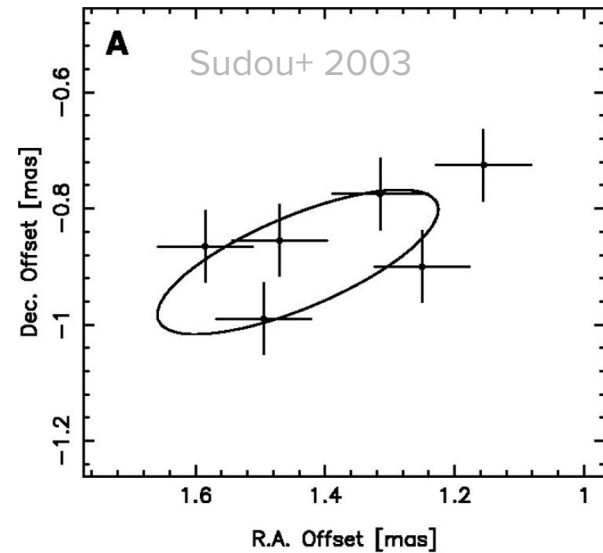
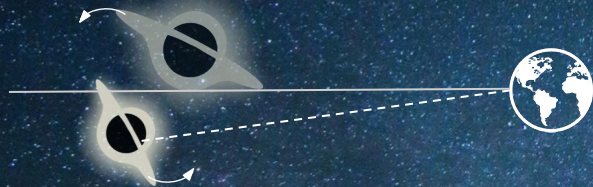
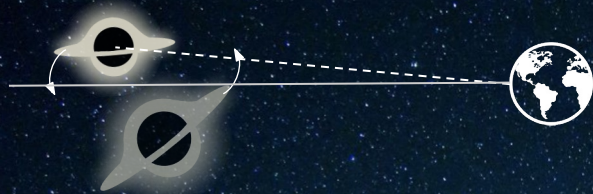


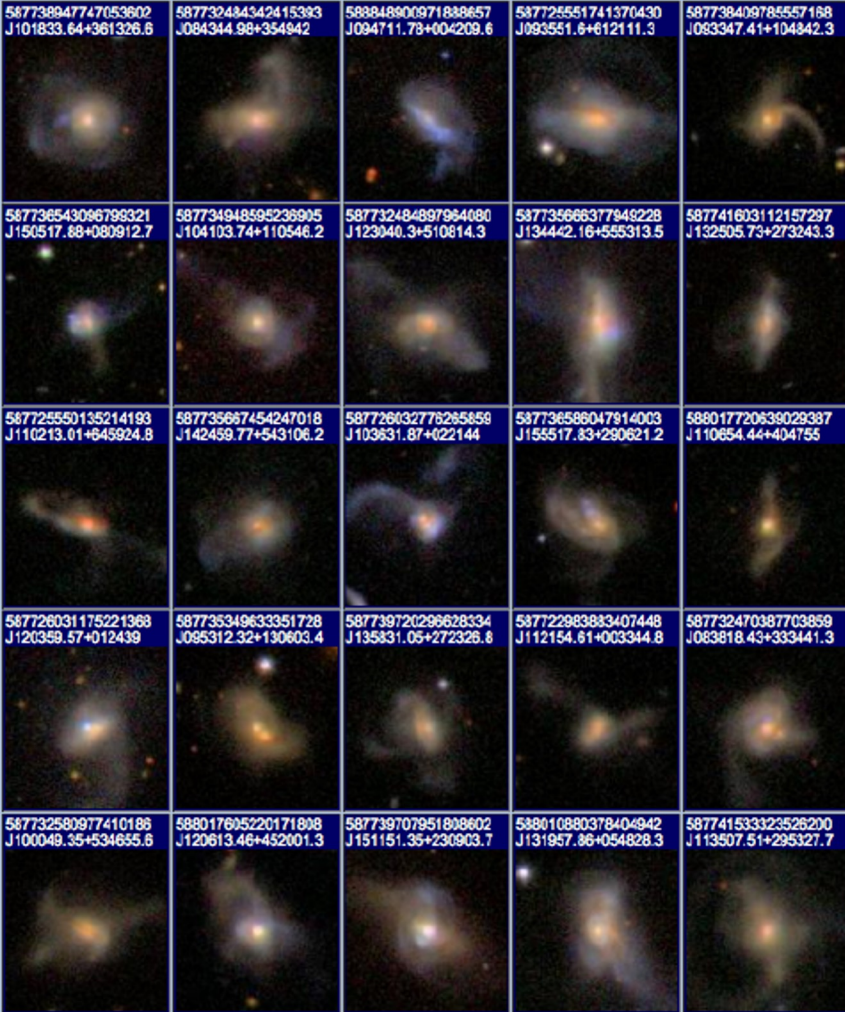
# Periodic Self Lensing

As BHs align on line-of-sight, one binary lenses the other and magnifies it's brightness



# Variable Position

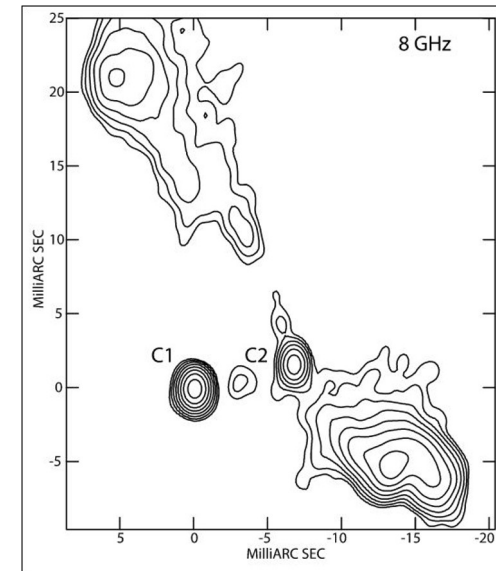




Evidence of past  
mergers

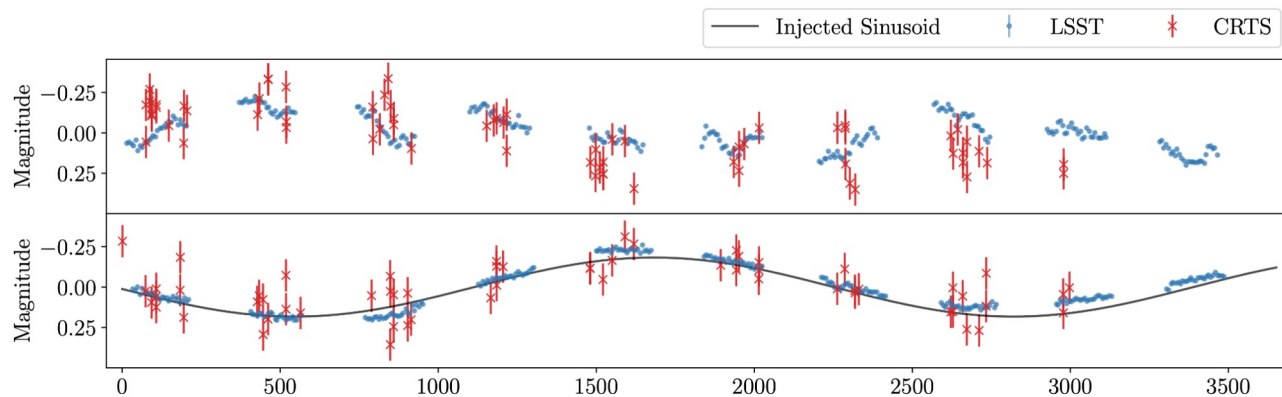
These methods do NOT  
indicate orbital frequency

Spatial Offsets

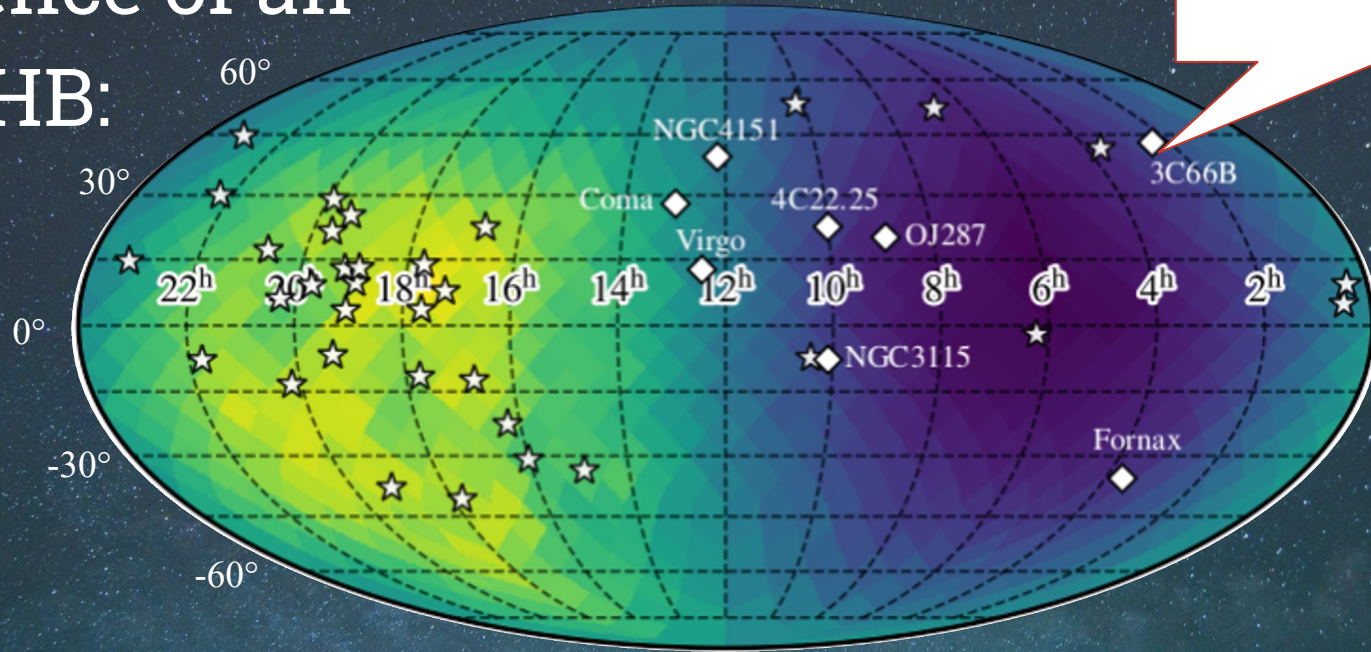


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Many signatures can easily be replicated by noise

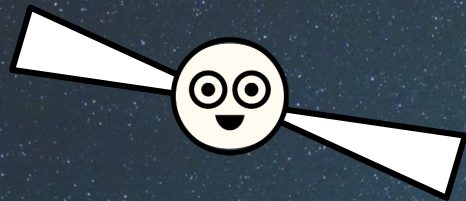


If we see  
evidence of an  
SMBHB:



We might want to look for a CW

# How PTAs work:



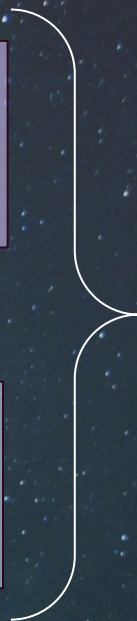
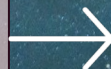
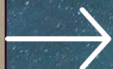
**Searching**  
Search for new pulsars

**Timing**  
Observe and time  
pulsars, make dataset

**Noise budget**  
Characterize noise,  
ISM mitigation

**Detection**  
Run and develop new  
detection analyses

**Astrophysics**  
Interpret GW limits, GW  
sources



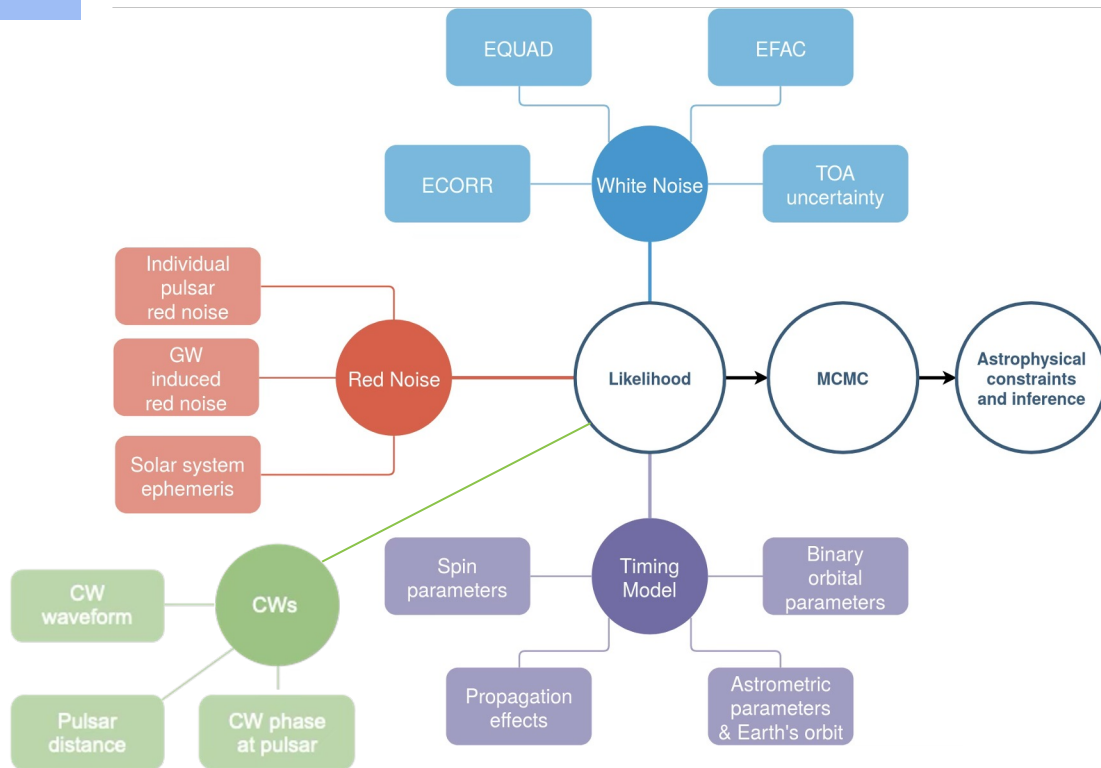
## Detection

Run and develop new  
detection analyses



In reality,  
things are more  
complicated

Can we make  
anything  
simpler?



# Multi-messenger astrophysics with PTAs

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If some of the GW parameters are constrained, it could be easier to detect the signals

$$\{\theta, \phi, f_{\text{gw}}, \Phi_0, \psi, i, \mathcal{M}, d_L, h_0\}$$

$$h_0 = \frac{2\mathcal{M}^{5/3} (\pi f_{\text{gw}})^{2/3}}{d_L}$$

If we see signatures, we would know:

- Galaxy coordinates
- Distance
- Frequency?
- Size?
- Inclination?

# Option #1: Constrain Priors

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Constant value prior for:

- Sky location
- Distance
- Frequency?

Pros:

- Simpler model → faster analysis, more sensitive
- Make statements about particular systems

Cons:

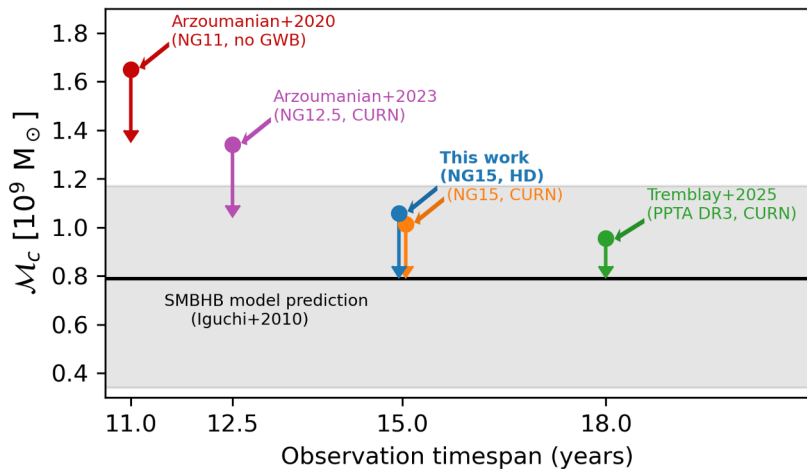
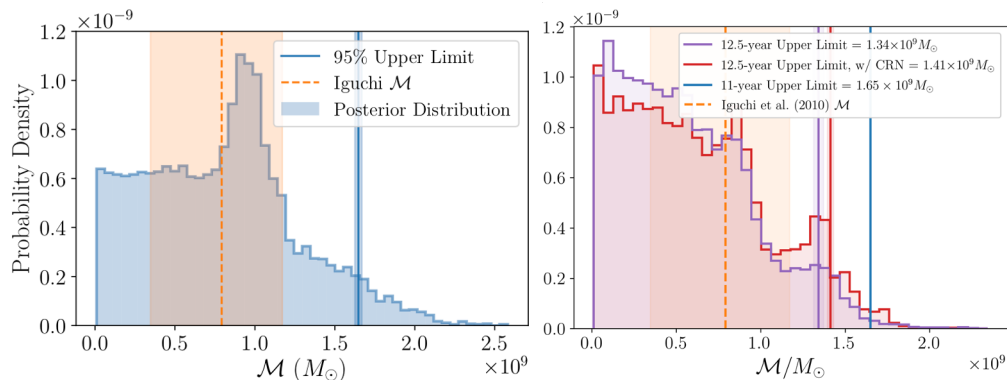
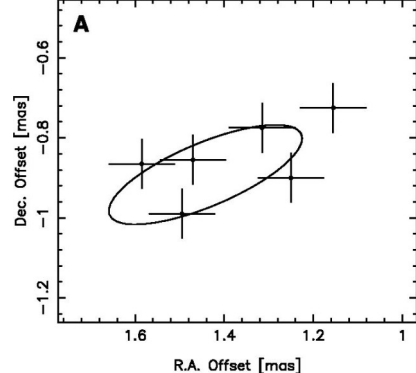
- Relies on assumptions and other observations
- Complexities with sky localization and repeated searches

# For example: 3C 66B

Classic EM SMBHB candidate with proposed GW frequency of 60.4 nHz

→ fix sky location, distance, and frequency to constant value

No evidence found in any search



# More sources:

Now extended to a catalog of sources  
for NG15

| Name                      | RA             | Dec            | z    | Period<br>[days] | Freq<br>[nHz] | $M_{\text{out}}$<br>[ $M_{\odot}$ ] | $\mathcal{M}_{\text{c}}^{\text{95\%}}$<br>[ $M_{\odot}$ ] | $h_{\text{95\%}}^{\text{95\%}}$ |
|---------------------------|----------------|----------------|------|------------------|---------------|-------------------------------------|-----------------------------------------------------------|---------------------------------|
| MCG 5-40-026 <sup>a</sup> | 17h 01m 07.80s | +29d 24m 24.6s | 0.04 | 1407             | 16.4          | $7.24 \times 10^6$                  | $1.29 \times 10^9$                                        | $5.38 \times 10^{-15}$          |
| SDSS J072908.71+400836.6  | 07h 29m 08.60s | +40d 08m 37.0s | 0.07 | 1612             | 14.4          | $2.63 \times 10^7$                  | $3.38 \times 10^8$                                        | $1.16 \times 10^{-14}$          |
| 2MASS J04352649-1643460   | 04h 35m 26.50s | -16d 43m 45.7s | 0.10 | 1369             | 16.9          | $6.03 \times 10^7$                  | $3.92 \times 10^9$                                        | $1.23 \times 10^{-14}$          |
| PGC 3096192               | 12h 50m 29.00s | +06d 36m 11.1s | 0.13 | 1561             | 14.8          | $1.15 \times 10^7$                  | $3.55 \times 10^8$                                        | $6.85 \times 10^{-15}$          |
| SDSS J110554.78+322953.7  | 11h 05m 54.80s | +32d 29m 54.1s | 0.15 | 1724             | 13.4          | $1.74 \times 10^8$                  | $4.52 \times 10^9$                                        | $8.38 \times 10^{-15}$          |
| HS 0423+0658              | 04h 26m 30.20s | +07d 05m 30.3s | 0.17 | 1123             | 20.6          | —                                   | $4.01 \times 10^9$                                        | $8.00 \times 10^{-15}$          |
| HS 2219+1944              | 22h 22m 21.10s | +19d 59m 48.1s | 0.21 | 1724             | 13.4          | —                                   | $3.87 \times 10^9$                                        | $4.46 \times 10^{-15}$          |
| SDSS J121018.34+015405.9  | 12h 10m 18.30s | +01d 5m 06.2s  | 0.22 | 1612             | 14.4          | $3.47 \times 10^6$                  | $4.12 \times 10^9$                                        | $5.05 \times 10^{-15}$          |
| SNU J13120+0641           | 13h 12m 04.70s | +06d 41m 07.6s | 0.24 | 1492             | 15.5          | $1.38 \times 10^9$                  | $6.54 \times 10^9$                                        | $1.01 \times 10^{-14}$          |
| SDSS J161013.67+311756.4  | 16h 10m 13.70s | +31d 17m 56.s  | 0.25 | 1724             | 13.4          | $8.23 \times 10^7$                  | $1.82 \times 10^9$                                        | $1.07 \times 10^{-15}$          |
| CT 638                    | 03h 18m 06.50s | -34d 26m 37.4s | 0.27 | 1514             | 15.3          | —                                   | $9.57 \times 10^9$                                        | $1.70 \times 10^{-14}$          |
| RXS J04117+1324           | 04h 11m 46.90s | +13d 24m 16.5s | 0.28 | 1850             | 12.5          | $1.45 \times 10^8$                  | $2.95 \times 10^9$                                        | $1.99 \times 10^{-15}$          |
| BZQJ1305-1033             | 13h 05m 33.00s | -10d 33m 19.1s | 0.29 | 1693             | 13.7          | $3.16 \times 10^8$                  | $5.25 \times 10^9$                                        | $5.30 \times 10^{-15}$          |
| SDSS J123821.84+030024.2  | 12h 38m 21.80s | +03d 00m 24.6s | 0.38 | 1249             | 18.5          | $8.32 \times 10^8$                  | $6.58 \times 10^9$                                        | $6.79 \times 10^{-15}$          |
| SDSS J153636.22+044127.0  | 15h 36m 36.20s | +04d 41m 26.9s | 0.38 | 1110             | 20.8          | $6.61 \times 10^8$                  | $6.33 \times 10^9$                                        | $6.92 \times 10^{-15}$          |
| SDSS J135225.80+132853.2  | 13h 52m 25.80s | +13d 28m 53.3s | 0.40 | 1754             | 13.2          | $5.62 \times 10^8$                  | $6.07 \times 10^9$                                        | $4.44 \times 10^{-15}$          |
| KUV 09484+3557            | 09h 51m 23.90s | +35d 42m 49.2s | 0.40 | 1162             | 19.9          | $2.04 \times 10^8$                  | $3.83 \times 10^9$                                        | $2.74 \times 10^{-15}$          |
| SDSS J141425.92+171811.2  | 14h 14m 25.90s | +17d 18m 11.6s | 0.41 | 1785             | 13.0          | $3.89 \times 10^8$                  | $2.50 \times 10^9$                                        | $9.77 \times 10^{-16}$          |
| SDSS J133631.45+175613.8  | 13h 36m 31.40s | +17d 56m 14.1s | 0.42 | 1561             | 14.8          | $1.07 \times 10^9$                  | $8.73 \times 10^9$                                        | $8.31 \times 10^{-15}$          |
| SDSS J224829.47+144418.0  | 22h 48m 29.40s | +14d 44m 18.4s | 0.42 | 1218             | 19.0          | $7.24 \times 10^8$                  | $3.52 \times 10^9$                                        | $2.14 \times 10^{-15}$          |
| RXS J10304+5516           | 10h 30m 25.0s  | +55d 16m 23.4s | 0.44 | 1514             | 15.3          | $2.69 \times 10^8$                  | $1.07 \times 10^{10}$                                     | $1.14 \times 10^{-14}$          |
| SDSS J140600.26+013252.2  | 14h 06m 00.30s | +01d 32m 52.4s | 0.45 | 1999             | 11.6          | $2.57 \times 10^8$                  | $8.63 \times 10^9$                                        | $6.32 \times 10^{-15}$          |
| SDSS J094715.56+631716.4  | 09h 47m 15.60s | +63d 17m 17.3s | 0.49 | 1724             | 13.4          | $1.66 \times 10^9$                  | $8.46 \times 10^9$                                        | $6.20 \times 10^{-15}$          |
| SDSS J114749.70+163106.7  | 11h 47m 49.70s | +16d 31m 06.8s | 0.55 | 1449             | 16.0          | $1.66 \times 10^8$                  | $1.32 \times 10^{10}$                                     | $1.25 \times 10^{-14}$          |
| SDSS J084146.19+503601.1  | 08h 41m 46.30s | +50d 36m 00.5s | 0.56 | 1693             | 13.7          | $2.75 \times 10^7$                  | $1.21 \times 10^{10}$                                     | $9.71 \times 10^{-15}$          |
| MS 10548-0335             | 10h 57m 22.30s | -03d 51m 31.3s | 0.56 | 892              | 26.0          | —                                   | $1.02 \times 10^{10}$                                     | $1.12 \times 10^{-14}$          |
| SDSS J161854.64+230859.1  | 16h 18m 54.60s | +23d 08m 59.3s | 0.56 | 1666             | 13.9          | $2.34 \times 10^8$                  | $7.33 \times 10^9$                                        | $4.21 \times 10^{-15}$          |
| SDSS J144754.62+132610.0  | 14h 47m 54.60s | +13d 26m 10.4s | 0.57 | 1960             | 11.8          | $3.8 \times 10^8$                   | $9.66 \times 10^9$                                        | $5.85 \times 10^{-15}$          |
| 6QZ J221925.1-305408      | 22h 19m 25.20s | -30d 54m 08.1s | 0.58 | 1407             | 16.4          | —                                   | $8.42 \times 10^9$                                        | $5.71 \times 10^{-15}$          |
| HS 0946+4845              | 09h 50m 00.70s | +48d 31m 29.9s | 0.59 | 1586             | 14.6          | $3.89 \times 10^8$                  | $1.38 \times 10^{10}$                                     | $1.18 \times 10^{-14}$          |
| HS 1715+2131              | 17h 17m 20.10s | +21d 28m 15.0s | 0.59 | 1249             | 18.5          | —                                   | $7.94 \times 10^9$                                        | $5.48 \times 10^{-15}$          |
| SDSS J134820.42+194831.5  | 13h 48m 20.40s | +19d 48m 31.9s | 0.59 | 1388             | 16.7          | $4.27 \times 10^7$                  | $8.78 \times 10^9$                                        | $6.00 \times 10^{-15}$          |
| SDSS J143820.60+055447.9  | 14h 38m 20.60s | +05d 54m 48.1s | 0.61 | 1850             | 12.5          | $1.55 \times 10^8$                  | $9.39 \times 10^9$                                        | $5.32 \times 10^{-15}$          |
| SDSS J125414.23+131348.1  | 12h 54m 14.20s | +13d 13m 48.4s | 0.66 | 1754             | 13.2          | $8.71 \times 10^8$                  | $9.69 \times 10^9$                                        | $5.36 \times 10^{-15}$          |
| SDSS J144755.57+100040.0  | 14h 47m 55.60s | +10d 00m 40.4s | 0.68 | 861              | 26.9          | $8.51 \times 10^8$                  | $7.39 \times 10^9$                                        | $5.26 \times 10^{-15}$          |
| RX J024252.3-232633       | 02h 42m 51.90s | -23d 26m 34.0s | 0.68 | 1817             | 12.7          | —                                   | $1.08 \times 10^{10}$                                     | $6.02 \times 10^{-15}$          |
| SDSS J082716.85+490534.0  | 08h 27m 16.90s | +49d 05m 34.9s | 0.68 | 1612             | 14.4          | $9.12 \times 10^8$                  | $1.61 \times 10^{10}$                                     | $1.25 \times 10^{-14}$          |
| SDSS J132103.41+123748.2  | 13h 21m 03.40s | +12d 37m 48.1s | 0.69 | 1538             | 15.1          | $8.13 \times 10^8$                  | $1.31 \times 10^{10}$                                     | $9.11 \times 10^{-15}$          |
| SBS 0920+590              | 09h 23m 58.70  | +58d 49m 06.3s | 0.71 | 648              | 35.7          | $5.75 \times 10^8$                  | $1.74 \times 10^{10}$                                     | $2.50 \times 10^{-14}$          |
| SDSS J221016.97+122123.9  | 22h 10m 17.00s | +12d 22m 14.0s | 0.72 | 1333             | 17.4          | $1.00 \times 10^9$                  | $7.90 \times 10^9$                                        | $4.10 \times 10^{-15}$          |
| SDSS J124044.49+231045.8  | 12h 40m 44.50s | +23d 10m 46.1s | 0.72 | 1428             | 16.2          | $8.71 \times 10^8$                  | $1.41 \times 10^{10}$                                     | $1.02 \times 10^{-14}$          |
| UM 234                    | 00h 23m 03.20s | +01d 15m 33.9s | 0.73 | 1817             | 12.7          | $1.55 \times 10^9$                  | $1.30 \times 10^{10}$                                     | $7.47 \times 10^{-15}$          |
| SDSS J152157.02+181018.6  | 15h 21m 57.00s | +18d 10m 19.2s | 0.73 | 1960             | 11.8          | $8.91 \times 10^7$                  | $1.17 \times 10^{10}$                                     | $5.94 \times 10^{-15}$          |
| 163107.34+560905.3        | 16h 31m 07.40s | +56d 09m 05.1s | 0.73 | 1724             | 13.4          | $2.40 \times 10^8$                  | $9.08 \times 10^9$                                        | $4.26 \times 10^{-15}$          |

<sup>a</sup>EM mass from Pal et al. (2024)

**Table 6.** Electromagnetic and GW-constrained upper limits on chirp mass and strain amplitude for candidate SMBHBs. EM-derived total masses are reported when available in [Graham et al. \(2015\)](#), except when indicated otherwise.

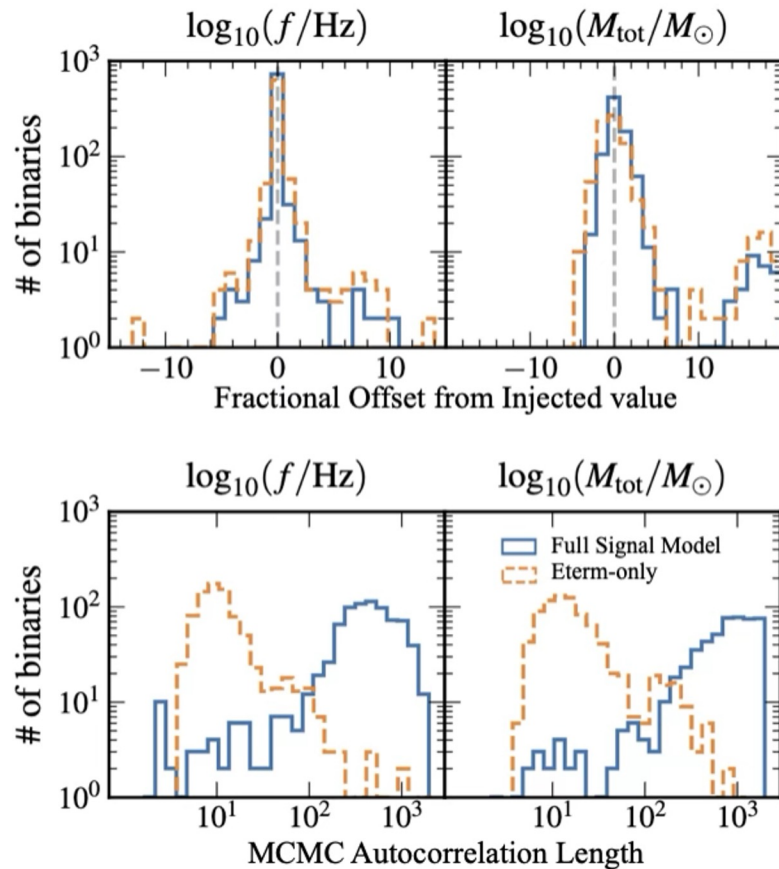
# Further Simplifications

Multi-messenger modeling allows simplifications to the GW signal model

$$\Delta s_{+,\times}(t) = \cancel{s_{+,\times}(t_p)} - s_{+,\times}(t)$$

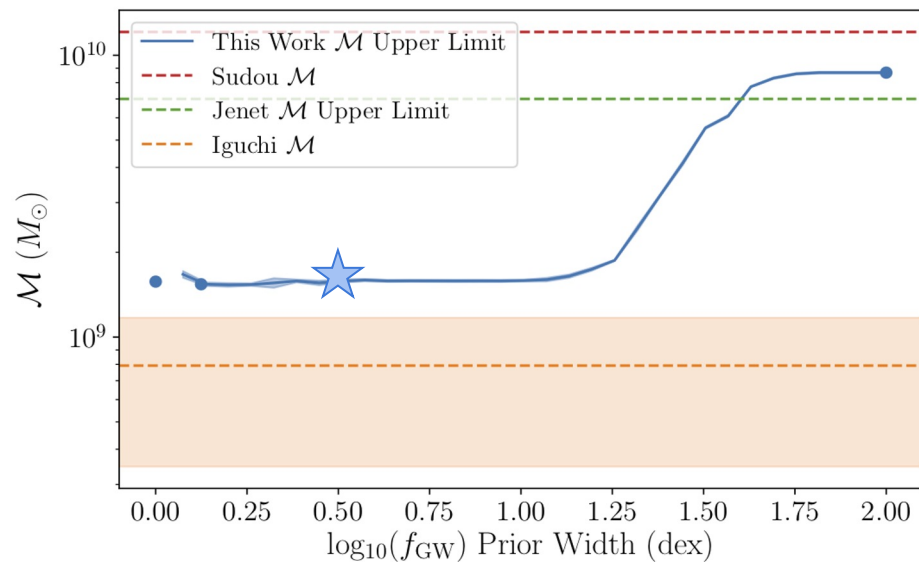
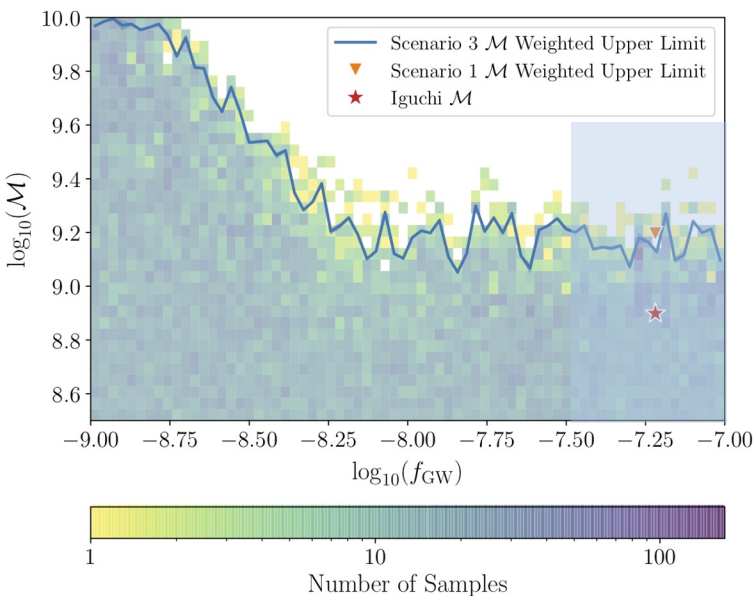
- Allows **significantly faster** analyses
- Critical expansion in advance of next-generation time-domain surveys

Figure Credit: Charisi+2024, inc CAW



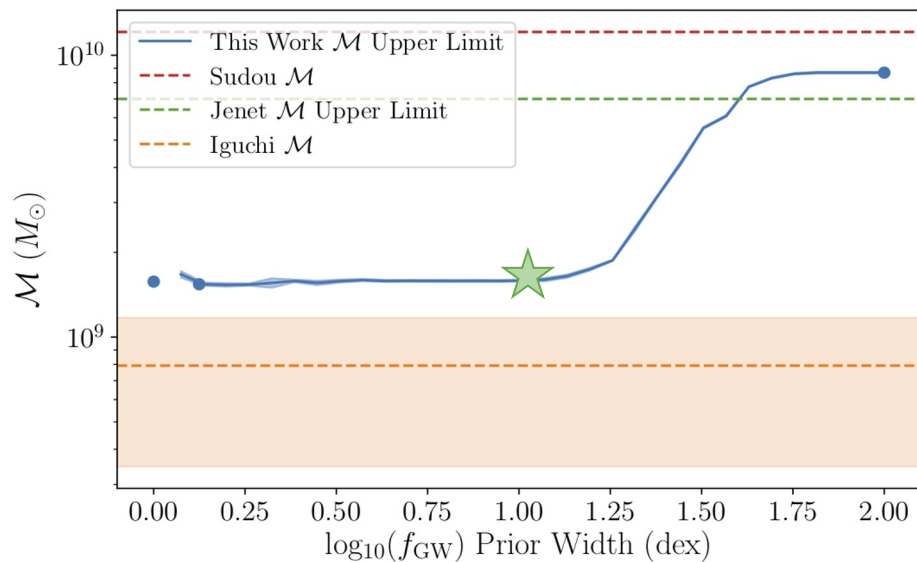
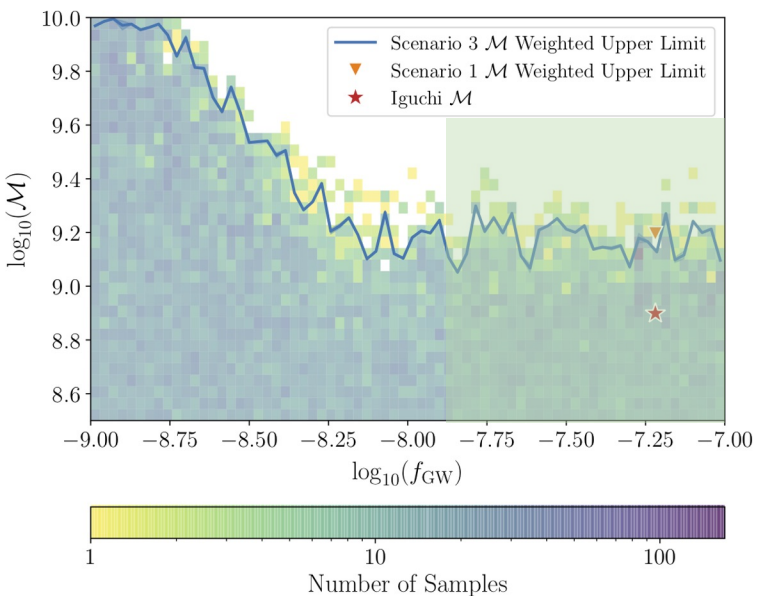
# A few variations:

What if we don't know a parameter exactly? We can give it a constrained, but not constant, prior



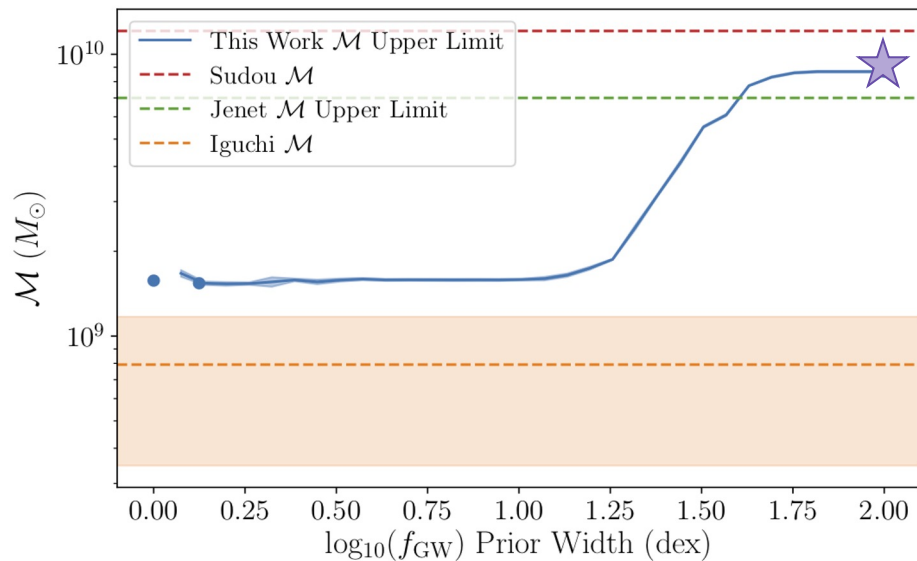
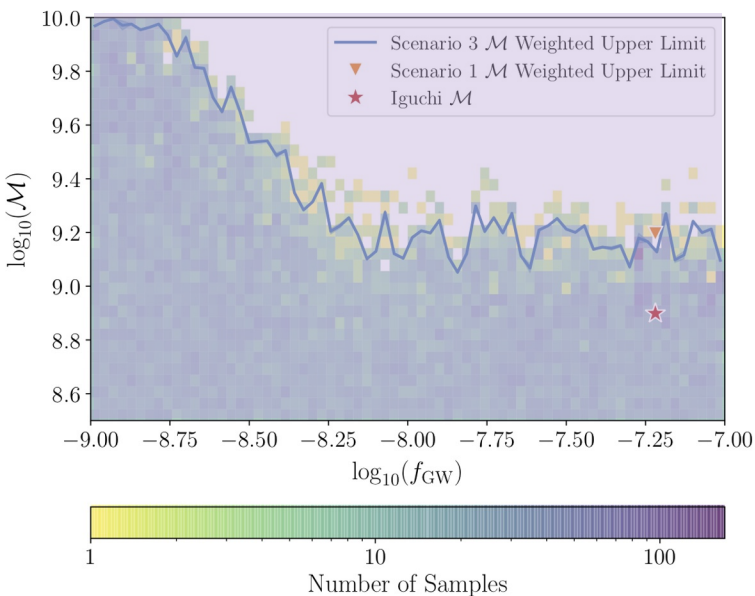
# A few variations:

What if we don't know a parameter exactly? We can give it a constrained, but not constant, prior



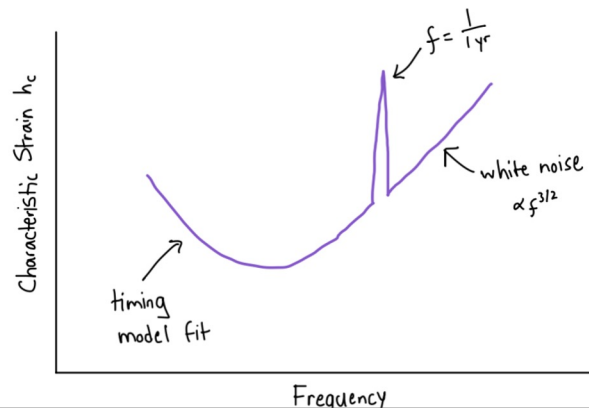
# A few variations:

What if we don't know a parameter exactly? We can give it a constrained, but not constant, prior



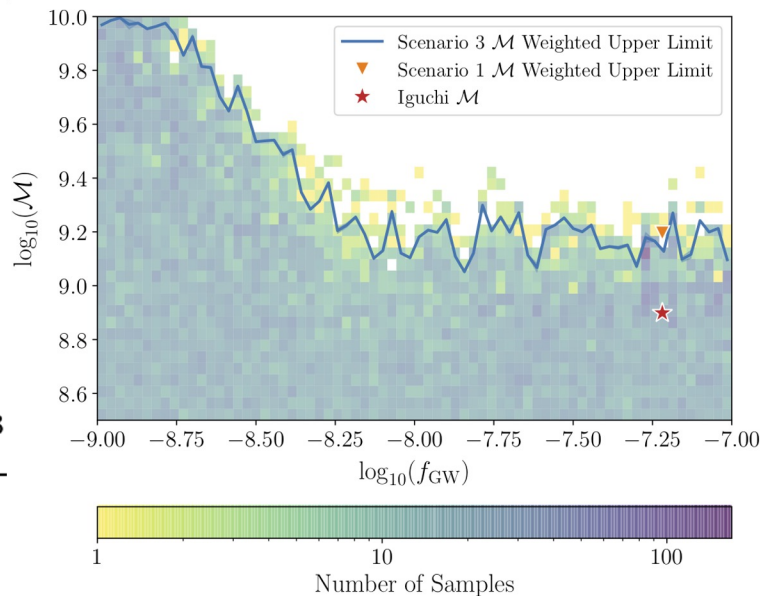
# One more bonus

From Sarah's lecture on GWs:

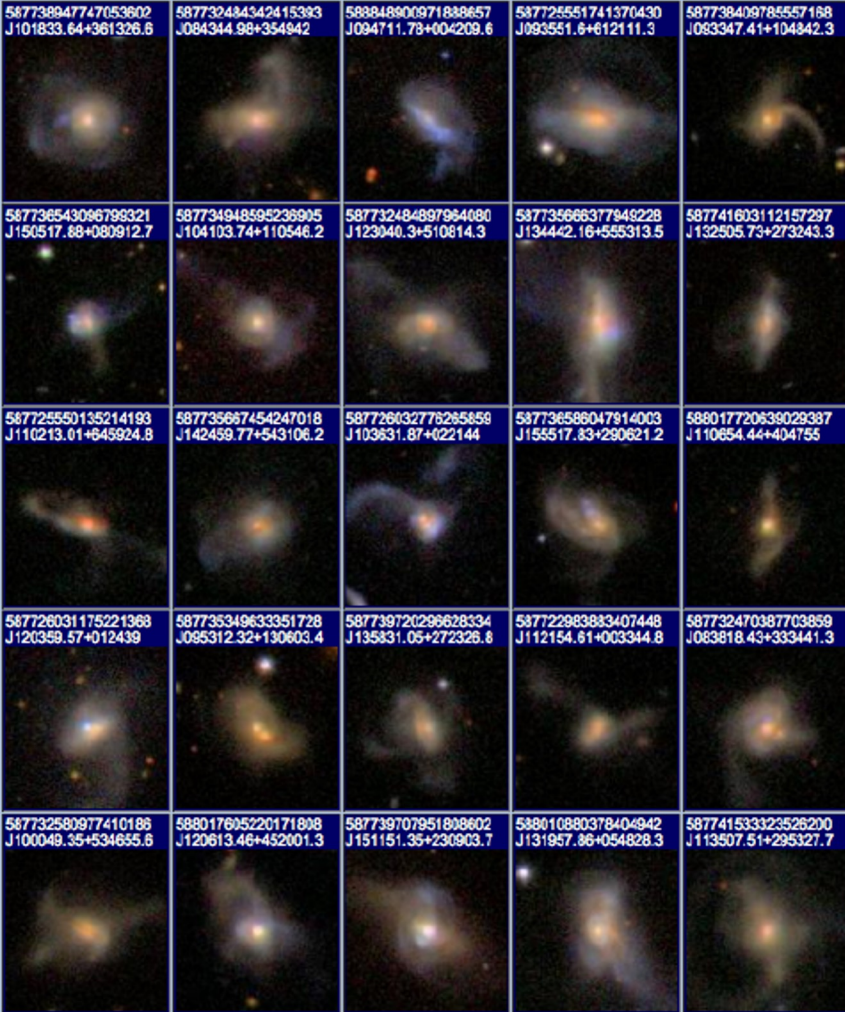


For white noise,  $S_r(f) \sim f^0 \Rightarrow h_c(f) \sim f^{3/2}$ .

$$h_0 = \frac{2\mathcal{M}^{5/3} (\pi f_{\text{gw}})^{2/3}}{d_L}$$



Scalings (and sensitivity) transform when searching directly in chirp mass

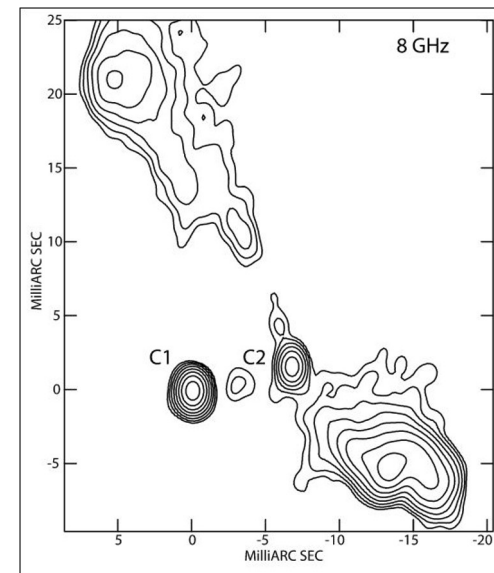


Evidence of past  
mergers

These methods do NOT  
indicate orbital frequency

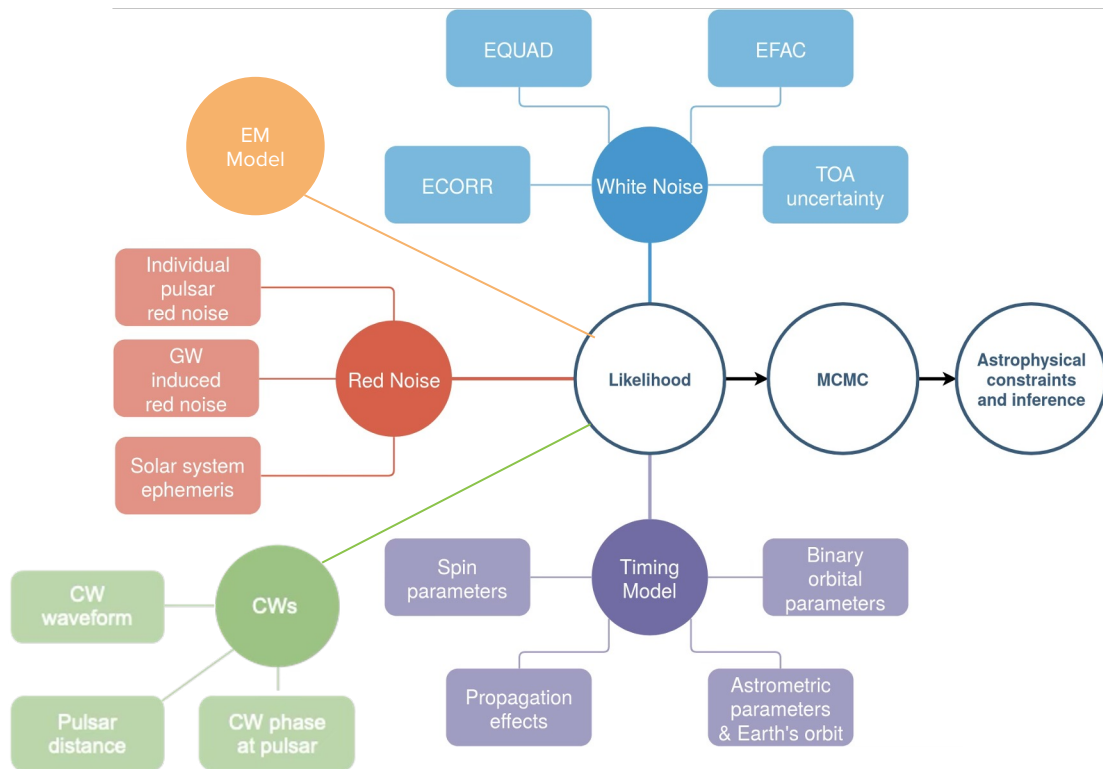
Spatial Offsets

Useful for sources like  
these!

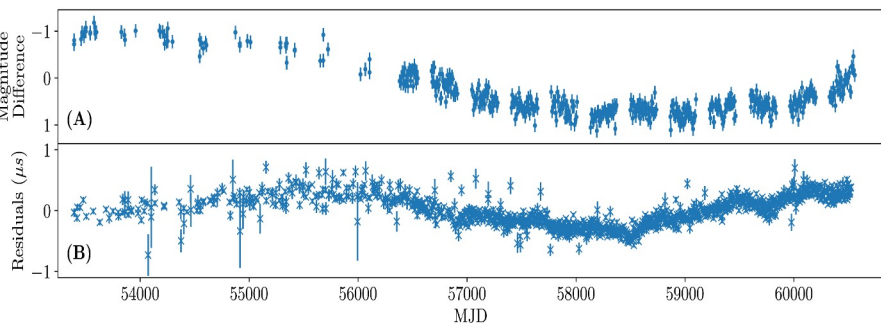


# Option #2: Joint Analysis

Adapt your likelihood to accept PTA and EM data at once



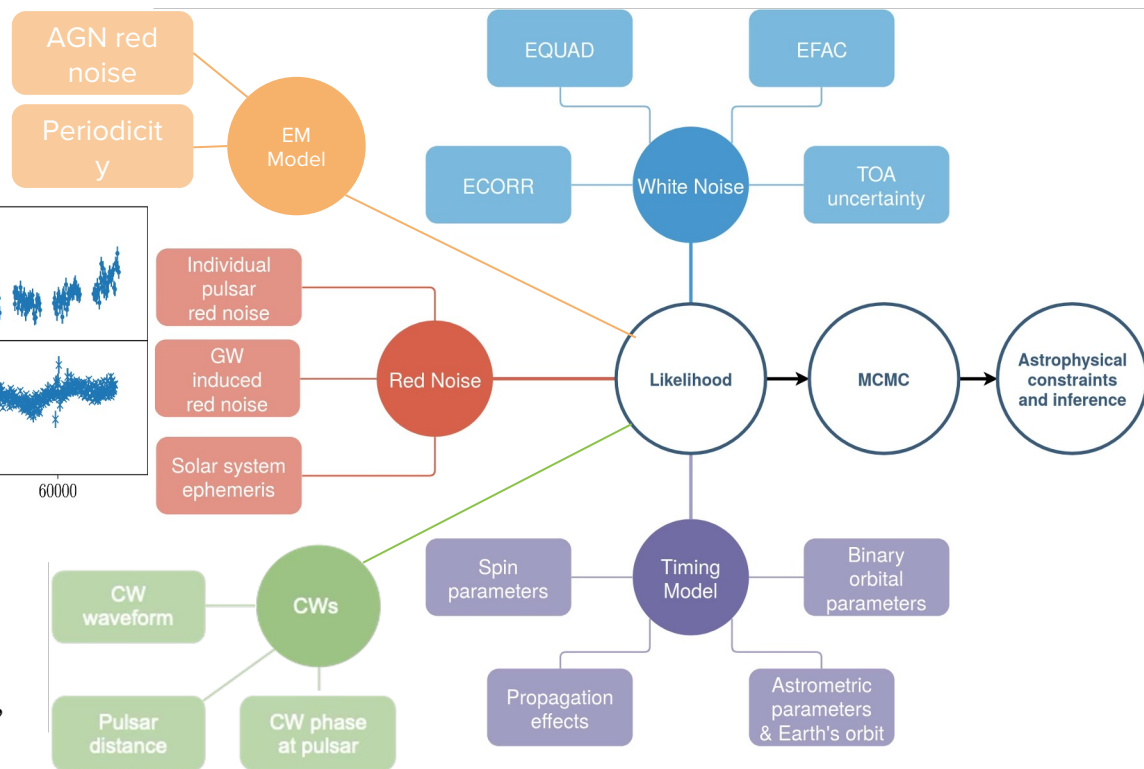
# For example: Periodic Quasars



$$\mathcal{L}_{\text{MMA}} = \mathcal{L}_{\text{PTA}} \mathcal{L}_{\text{EM}},$$

or more specifically,

$$\ln p(d_{\text{MMA}} | \vec{\theta}_{\text{MMA}}) = \ln p(d_{\text{PTA}} | \vec{\theta}_{\text{PTA}}) + \ln p(d_{\text{EM}} | \vec{\theta}_{\text{EM}}),$$



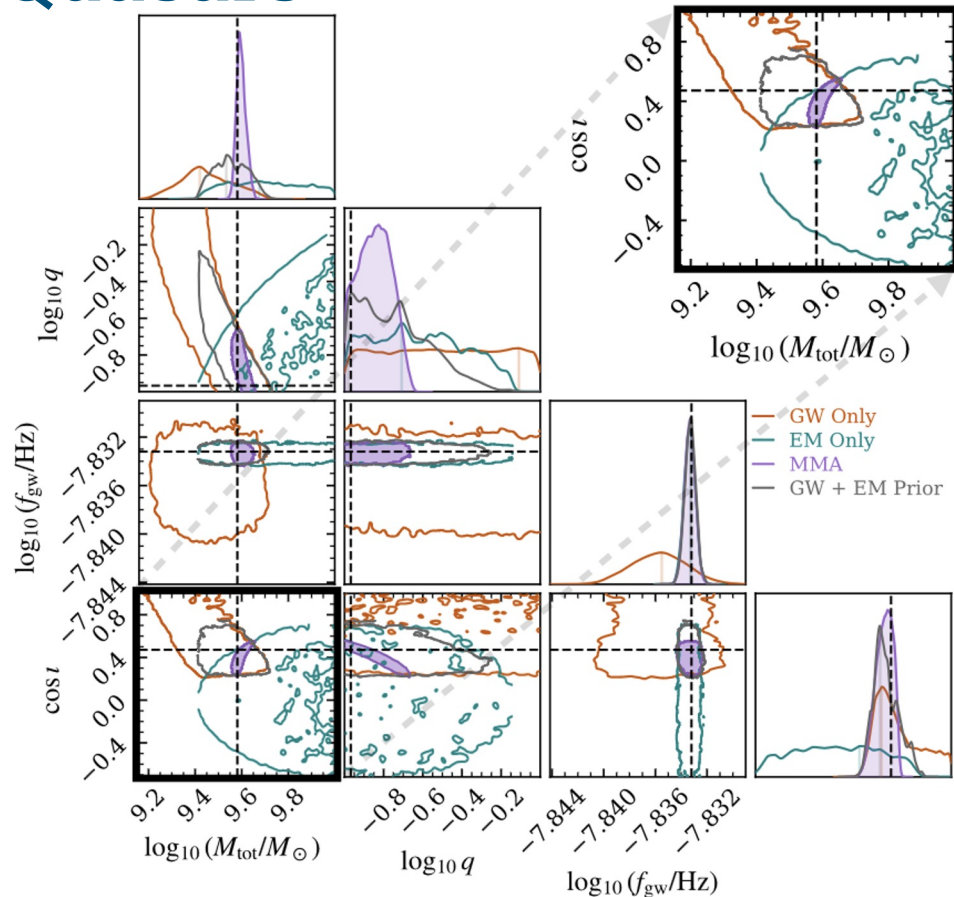
# For example: Periodic Quasars

## Pros:

- Related parameters help constrain each other (ex: period)

## Cons:

- More complex model  $\rightarrow$  slower
- Relies on assuming an EM model



# MMA for PTAs

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We've come a very long way!

- We've now placed MM limits on dozens of candidates

Lots more to do:

- More robust EM models and analyses
- CW search improvements

